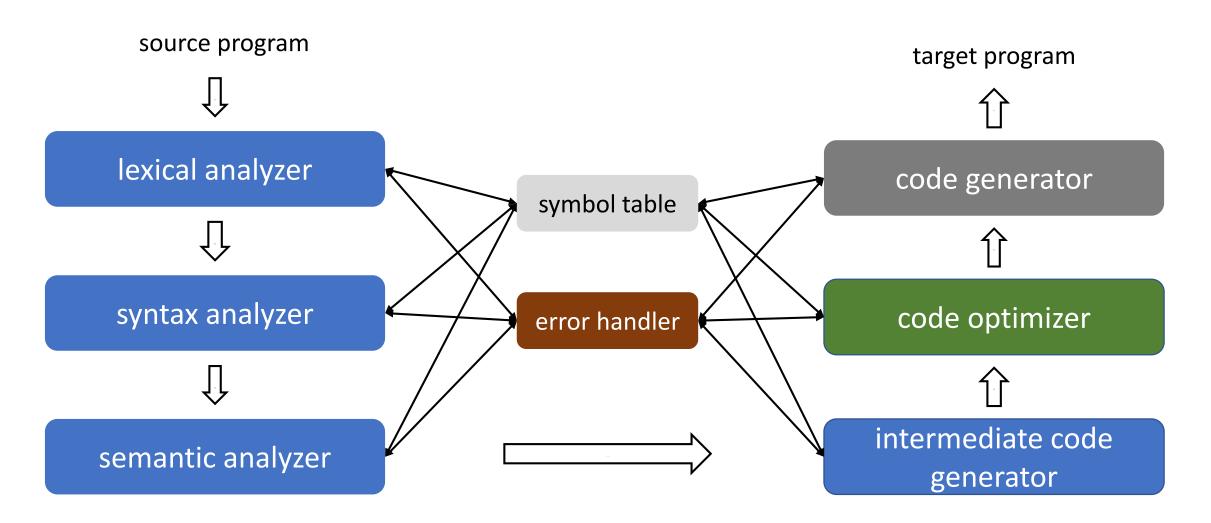
# CS 335: Semantic Analysis

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# An Overview of Compilation



# Beyond Scanning and Parsing

#### • Example 1

```
std::string x;
int y;
y = x + 3
```

#### • Example 2

```
int a, b;
a = b + c
```

```
int dot_prod(int x[], int y[]) {
  int d, i;
  d = 0;
  for (i=0; i<10; i++)
    d += x[i]*y[i];
  return d;
main() {
  int p, a[10], b[10];
  p = dot_prod(a,b);
```

# Beyond Scanning and Parsing

- A compiler must do more than just recognize whether a sentence belongs to a programming language grammar
  - An input program can be grammatically correct but may contain other errors that prevent compilation
  - Lexer and parser cannot catch all program errors
- Some language features cannot be modeled using context-free grammar (CFG)
  - Whether a variable has been declared before use?
  - Parameter types and numbers match in the declaration and use of a function
  - Types match on both sides of an assignment

#### Limitations with CFGs

#### $ProcedureBody \rightarrow Declarations Executables$

- CFGs deal with syntactic categories rather than specific words
  - Grammar can specify the positions in an expression where a variable name may occur
- Enforcing the "declare before use" rule requires knowledge that cannot be encoded in a CFG
  - CFG cannot match one instance of a variable name with another

## Questions That Compiler Needs to Answer

- Has a variable been declared?
- What is the type and size of a variable?
- Is the variable scalar or an array?
- Is an array access A[i][j][k] consistent with the declaration?
- Does the name "x" correspond to a variable or a function?
- If x is a function, how many arguments does it take?
- What kind of value, if any, does a function x return?
- Are all invocations of a function consistent with the declaration?
- Track inheritance relationship
- Ensure that classes and its methods are not multiply defined

Questions

# Questions That Compiler Needs to Answer

$$x \leftarrow y + z$$

$$x \leftarrow a + b$$

Compilers need to understand the structure of the computation to **translate** the input program

# Semantic Analysis

- Finding answers to these questions is part of the semantic analysis phase
  - For example, ensure variable are declared before their uses and check that each expression has a correct type
  - These are static semantics of languages

# Checking Dynamic Semantics

- Dynamic semantics of languages need to be checked at run time
  - Whether an overflow will occur during an arithmetic operation?
  - Whether array bounds will be exceeded during execution?
  - Whether recursion will exceed stack limits?
- Compilers can generate code to check dynamic semantics

```
int dot_prod(int x[], int y[]) {
  int d, i;
  d = 0;
  for (i=0; i<10; i++)
    d += x[i]*y[i];
  return d;
main() {
  int p; int a[10], b[10];
  p = dot_prod(a,b);
```

# How does a compiler answer these questions?

- Compilers track additional information for semantic analysis
  - For example, types of variables, function parameters, and array dimensions
    - Type information is stored in the symbol table or the syntax tree
  - Used not only for semantic validation but also for subsequent phases of compilation
  - The information required may be non-local in some cases

 Semantic analysis can be performed during parsing or in another pass that traverses the IR produced by the parser

# How does a compiler answer these questions?

Use formal methods like context-sensitive grammars

Use ad-hoc techniques using symbol table

- Static semantics of PL can be specified using attribute grammars
  - Attribute grammars are extensions of context-free grammars

# Attribute Grammar Framework

# Syntax-Directed Definition

- A syntax-directed definition (SDD) is a context-free grammar with rules and attributes
  - A SDD specifies the values of attributes by associating semantic rules with the grammar productions

Production	Semantic Rule
$E \rightarrow E_1 + T$	$E.code = E_1.code  T.code  " + "$

Attribute grammars are SDDs with no side effects

# Syntax-Directed Definition

- Generalization of CFG where each grammar symbol has an associated set of attributes
  - Let G = (T, NT, S, P) be a CFG and let  $V = T \cup NT$
  - Every symbol  $X \in V$  is associated with a set of attributes (for e.g., denoted by X. a and X. b)
  - Each attribute takes values from a specified domain (finite or infinite), which
    is its type
    - Typical domains of attributes are, integers, reals, characters, strings, booleans, and structures
  - New domains can be constructed from given domains by mathematical operations such as cross product and map
- Values of attributes are computed by semantic rules

# Example

 Consider a grammar for signed binary numbers

```
\begin{array}{l} number \rightarrow sign \ list \\ sign \rightarrow +| \ - \\ list \rightarrow list \ bit \ | \ bit \\ bit \rightarrow 0 \ | \ 1 \end{array}
```

• Build attribute grammar that annotates *Number* with the value it represents

# Example

 Consider a grammar for signed binary numbers

```
number \rightarrow sign\ list
sign \rightarrow +|-
list \rightarrow list\ bit\ |\ bit
bit \rightarrow 0\ |\ 1
```

• Build attribute grammar that annotates *number* with the value it represents

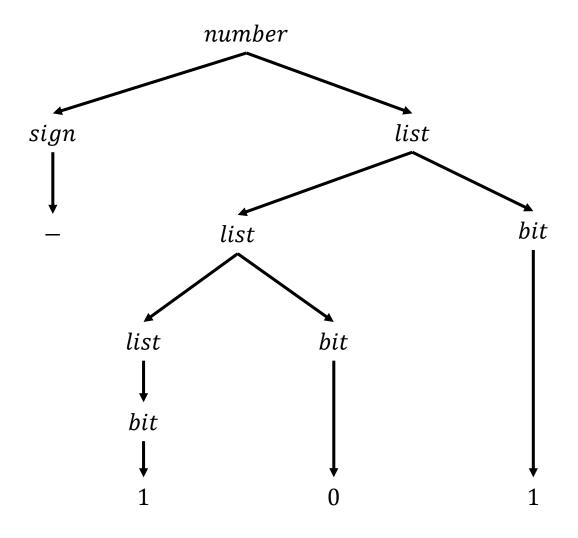
Associate attributes with grammar symbols

Symbol	Attributes
number	val
sign	neg
list	pos, val
bit	pos, val

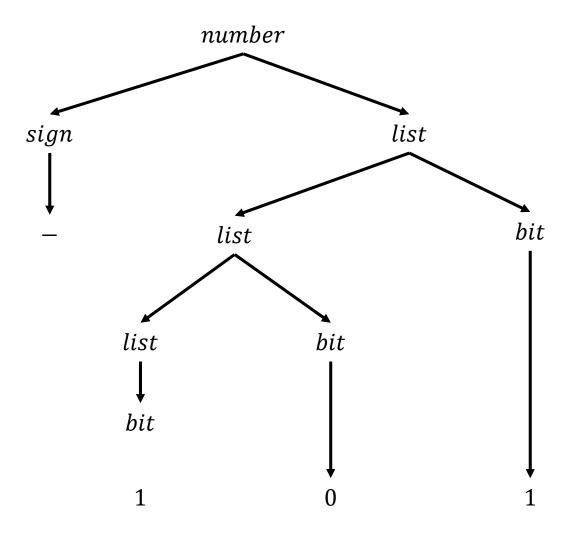
# Example Attribute Grammar

Production	Attribute Rule
number → sign list	list.pos = 0 $if sign.neg:$ $number.val = -list.val$ $else:$ $number.val = -list.val$
$sign \rightarrow +$	sign.neg = false
$sign \rightarrow -$	sign.neg = true
$list \rightarrow bit$	bit.pos = list.pos list.val = bit.val
$list_0 \rightarrow list_1 bit$	$list_1.pos = list_0.pos + 1$ $bit.pos = list_0.pos$ $list_0.val = list_1.val + bit.val$
$bit \rightarrow 0$	bit. val = 0
$bit \rightarrow 1$	$bit. val = 2^{bit.pos}$

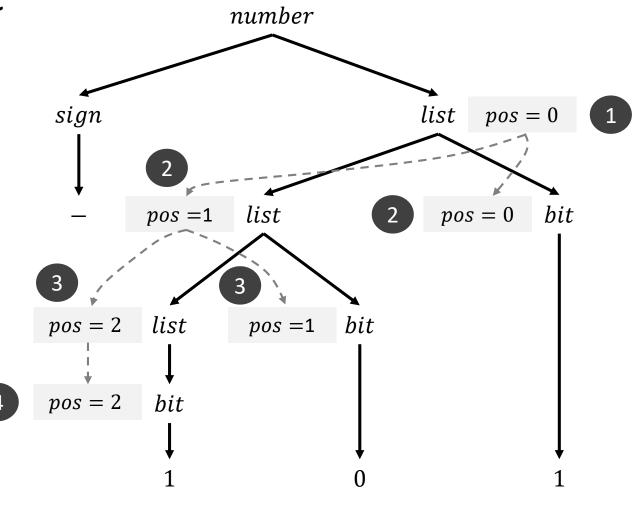
#### Parse Tree



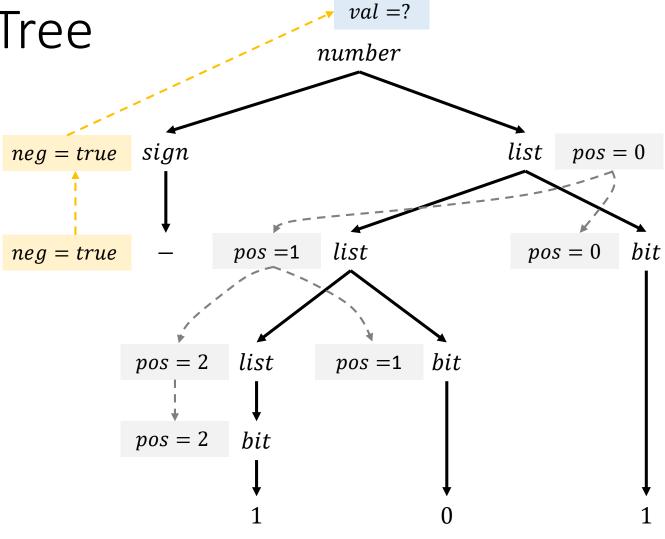
 A parse tree showing the value(s) of its attribute(s) is called an annotated parse tree



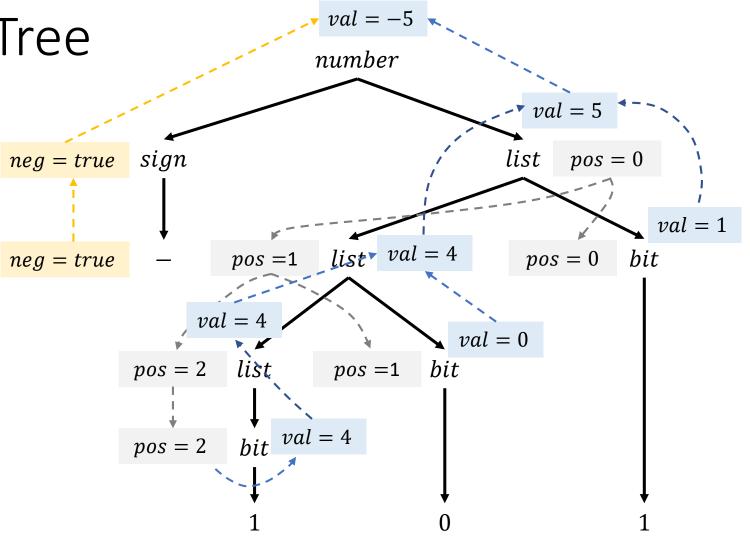
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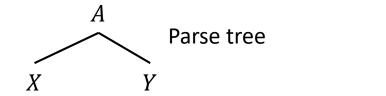


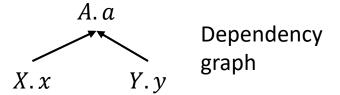
# Dependency Graph

- If an attribute b depends on an attribute c then the semantic rule for b must be evaluated after the semantic rule for c
- The dependencies among the nodes are depicted by a directed graph called dependency graph

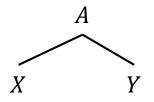
# Dependency Graph

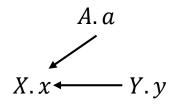
• Suppose A.a = f(X.x, Y.y) is a semantic rule for  $A \rightarrow XY$ 





• Suppose X.x = f(A.a, Y.y) is a semantic rule for  $A \rightarrow XY$ 





# Construct Dependency Graph

for each node n in the parse tree do for each attribute a of the grammar symbol do construct a node in the dependency graph for a

```
for each node n in the parse tree do for each semantic rule b=f(c_1,c_2,...,c_k) do for i=1 to k do construct an edge from c_i to b
```

// Associated with production at node n

# Evaluating an SDD

- In what order do we evaluate attributes?
  - SDDs do not specify any order of evaluation
  - We must evaluate all the attributes upon which the attribute of a node depends
  - Any topological sort of dependency graph gives a valid order in which semantic rules must be evaluated

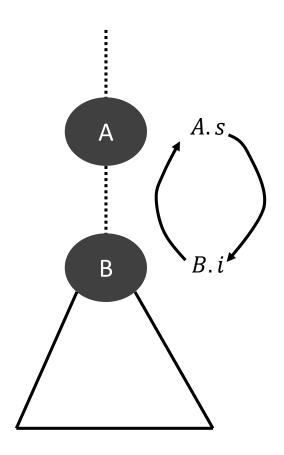
 For SDD's with both synthesized and inherited attributes, there is no guarantee of an order of evaluation existing

# Evaluating an SDD

- Parse tree method
  - Use topological sort of the dependency graph to find the evaluation order
- Rule-based method
  - Semantic rules are analyzed and order of evaluation is predetermined
- Oblivious method
  - Evaluation order ignores the semantic rules

# Circular Dependency of Attributes

Production	Semantic Rules
$A \rightarrow B$	A.s = B.i
	B.i = A.s + 1



## Types of Nonterminal Attributes

#### Synthesized

- Value of a synthesized attribute for a nonterminal A at a node N is computed from the values of children nodes and N itself
- ullet Defined by a semantic rule associated with a production at N such that the production has A as its head

#### Inherited

- Value of an inherited attribute for a nonterminal B at a node N is computed from the values at N's parent, N itself, and N's siblings
- ullet Defined by a semantic rule associated with the production at the parent of N such that the production has B in its body

# Syntax-Directed Definition

- A grammar production  $A \to \alpha$  has an associated semantic rule  $b = f(c_1, c_2, ..., c_k)$ 
  - b is a synthesized attribute of A and  $c_1, c_2, ..., c_k$  are attributes of symbols in the production
  - b is an inherited attribute of a symbol in the body, and  $c_1, c_2, ..., c_k$  are attributes of symbols in the production
- Start symbol does not have inherited attributes

#### Terminal Attributes

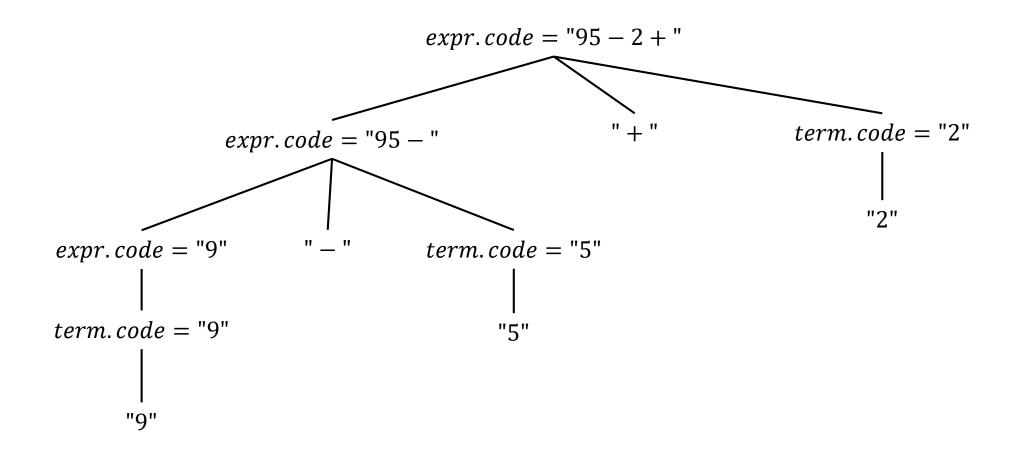
- Terminals can have synthesized attributes, but not inherited attributes
- Attributes for terminals have lexical values that are supplied by the lexical analyzer

#### Postfix Notation

- Postfix notation for an expression E is defined inductively
  - If E is a variable or constant, then postfix notation is E
  - If  $E = E_1 \text{ op} E_2$  where op is any binary operator, then the postfix notation is  $E_1' E_2' \text{ op}$ , where  $E_1'$  and  $E_2'$  are postfix notations for  $E_1$  and  $E_2$  respectively
  - If  $E = (E_1)$ , then postfix notation for  $E_1$  is the notation for E

### SDD for Infix to Postfix Translation

Production	Semantic Rules
$expr \rightarrow expr_1 + term$	$expr.code = expr_1.code  term.code  "+"$
$expr \rightarrow expr_1 - term$	$expr.code = expr_1.code  term.code  "-"$
$expr \rightarrow term$	expr.code = term.code
$term \rightarrow 0 \mid 1 \mid \mid 9$	term.code = "0" term.code = "1"  term.code = "9"



# Types of SDDs

- Arbitrary SDDs can have cycles
- Cycles need to be avoided
  - Can no longer meaningfully proceed with evaluation
  - Expensive to detect
- Two types of SDDs guarantee no cycles
  - S-attributed and L-attributed

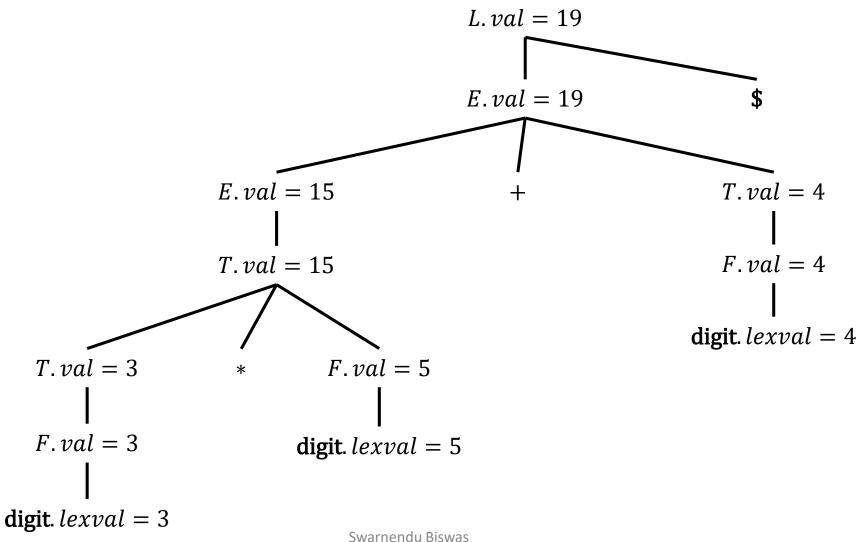
#### S-Attributed Definition

- An SDD that involves only synthesized attributes is called S-attributed definition
  - Each rule computes an attribute for the head nonterminal from attributes taken from the body of the production
- Semantic rules in a S-attributed definition can be evaluated by a bottom-up or postorder traversal of the parse tree
  - An S-attributed SDD can be implemented naturally in conjunction with an LR parser

# Example SDD

Production	Semantic Rules
$L \to E $ \$	L.val = E.val
$E \rightarrow E_1 + T$	$E.val = E_1.val + T.val$
$E \rightarrow T$	E.val = T.val
$T \to T_1 * F$	$T.val = T_1.val \times F.val$
$T \to F$	T.val = F.val
$F \to (E)$	F.val = E.val
F o digit	F.val = digit. lexval

## Annotated Parse Tree for 3 \* 5 + 4 \$

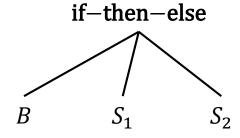


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# Abstract Syntax Tree (AST)

- Condensed form of a parse tree used for representing language constructs
  - ASTs do not check for string membership in the language for a grammar
  - ASTs represent relationships between language constructs, do not bother with derivations

$$S \to \mathbf{if} P \mathbf{then} S_1 \mathbf{else} S_2$$



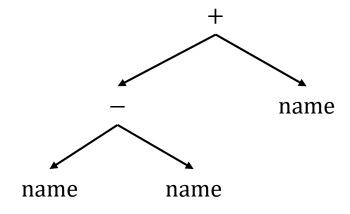
Parse trees are also called concrete syntax trees

# Parse Tree and Abstract Syntax Tree

#### **Parse Tree**

#### ExprTerm Expr Expr TermFactor Term Factor name Factor name name

#### **Abstract Syntax Tree**

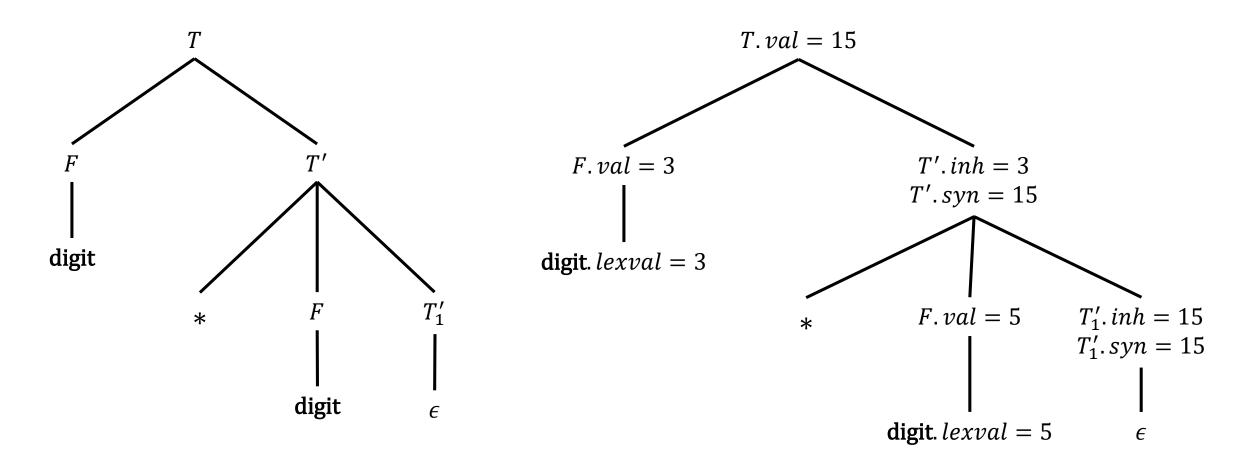


## Inherited Attributes

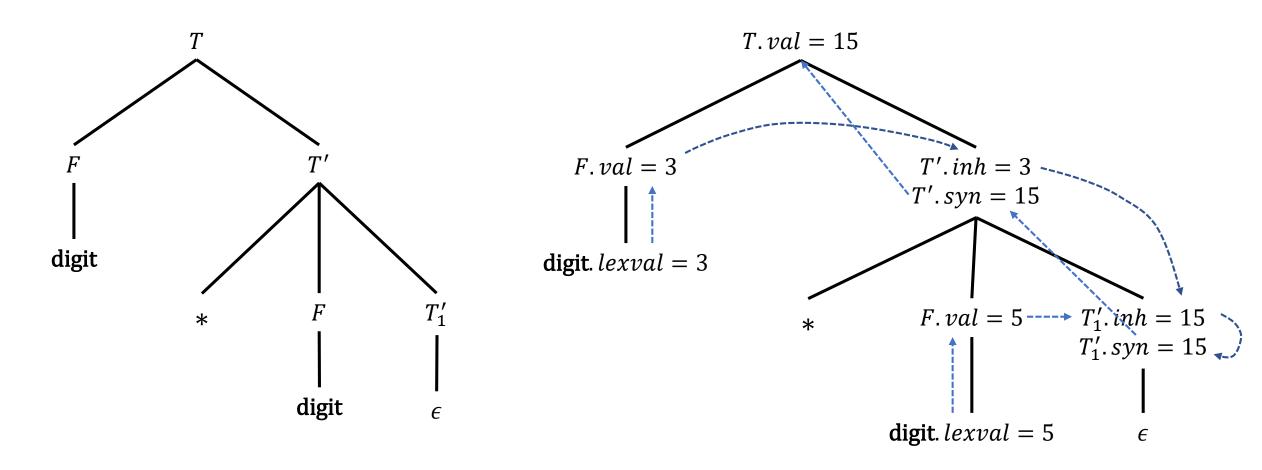
• Useful when the structure of the parse tree **does not match** the abstract syntax of the source code

Production	Semantic Rules
$T \to FT'$	T'.inh = F.val T.val = T'.syn
$T' \to *FT'_1$	$T'_1.inh = T'.inh \times F.val$ $T'.syn = T'_1.syn$
$T'  o \epsilon$	T'.syn = T'.inh
F o digit	F.val = digit. lexval

## Parse Tree and Annotated Parse Tree for 3 \* 5



## Parse Tree and Annotated Parse Tree for 3 \* 5

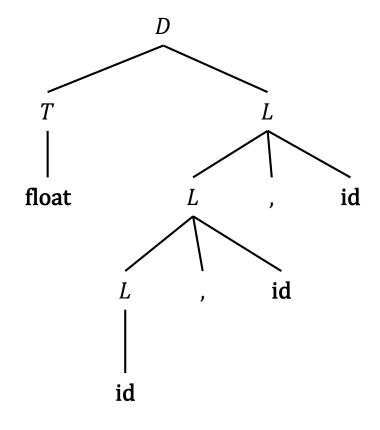


# Another Example

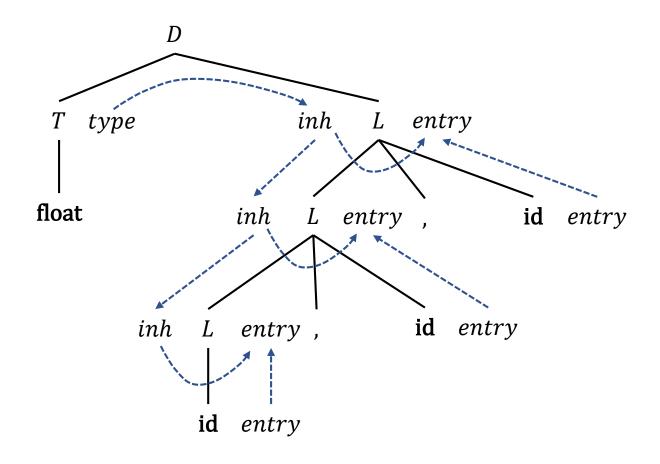
Production	Semantic Rules
$D \to TL$	L.in = T.type
$T \rightarrow float$	T.type = float
$T \rightarrow \mathbf{int}$	T.type = int
$L \rightarrow L_1$ , id	$L_1.in = L.in; addtype(id.entry, L.in)$
$L \rightarrow id$	addtype(id.entry, L.in)

addtype() installs L.in as the type of the symbol table object pointed to by id.entry

Parse Tree for "float x, y, z"



# Dependency Graph for float x, y, z



## **Evaluating S-Attributed Definitions**

 Attributes can be evaluated with a postorder traversal of the parse tree

```
postorder(N) {
    for (each child C of N, from left to right)
        postorder(C)
    evaluate the attributes associated with node N
}
```

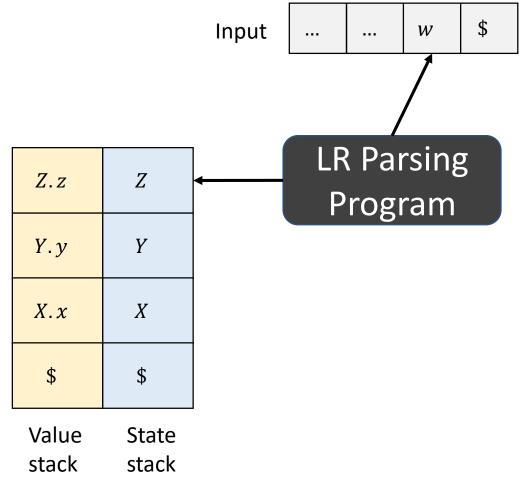
### Notes about Inherited Attributes

- Always possible to rewrite a SDD to use only synthesized attributes
  - Inherited attributes can be simulated with synthesized attributes
- May be more logical to use both synthesized and inherited attributes
- Inherited attributes usually cannot be evaluated by a simple preorder traversal of the parse tree
  - Attributes may depend on both left and right siblings!
  - Attributes that do not depend from right children can be evaluated by a preorder traversal

# Bottom-up Evaluation of S-Attributed Definitions

• Suppose  $A \rightarrow XYZ$ , and semantic rule is A.a = f(X.x, Y.y, Z.z)

- Can be computed during bottom-up parsing
  - On reduction, value of new synthesized attribute A. a is computed from the attributes on the stack
  - Extend stack to hold values



# Example S-Attributed Definition

Production	Semantic Rules
$L \to E $ \$	L.val = E.val
$E \rightarrow E_1 + T$	$E.val = E_1.val + T.val$
$E \rightarrow T$	E.val = T.val
$T \to T_1 * F$	$T.val = T_1.val \times F.val$
$T \to F$	T.val = F.val
$F \to (E)$	F.val = E.val
F  o digit	F.val = digit. lexval

# Bottom-up Evaluation of S-Attributed Definitions

Value	State	Input	Action
\$	\$	3 * 5 + 4\$	Shift
\$3	\$digit	* 5 + 4\$	Reduce by $F \rightarrow \mathbf{digit}$
\$3	F	* 5 + 4\$	Reduce by $T \to F$
\$3	T	* 5 + 4\$	Shift
\$3	\$ <i>T</i> *	5 + 4\$	Shift
\$3 5	T * digit	+4\$	Reduce by $F \rightarrow \mathbf{digit}$
\$3 5	T * F	+4\$	Reduce by $T \to T * F$
\$15	T	+4\$	Reduce by $E \rightarrow T$
\$15	\$ <i>E</i>	+4\$	Shift
\$15	\$E +	4\$	Shift
\$15 4	E + digit	\$	Reduce by $F \rightarrow \mathbf{digit}$
\$15 4	\$E + F	\$	Reduce by $T \to F$
\$15 4	\$E + T	\$	Reduce by $E \rightarrow E + T$
\$19	\$ <i>E</i>	\$	

## L-Attributed Definitions

- Each attribute must be either
  - I. Synthesized
  - II. Suppose  $A \rightarrow X_1X_2 \dots X_n$  and  $X_i$ . a is an inherited attribute.  $X_i$ . a can be computed using
    - a) Only inherited attributes from A, or
    - b) Either inherited or synthesized attributes associated with  $X_1, ..., X_{i-1}$ , or
    - c) Inherited or synthesized attributes associated with  $X_i$ .

Production	Semantic Rules
$T \to FT'$	T'.inh = F.val T.val = T'.syn
$T' \to *FT'_1$	$T'_1$ . $inh = T'$ . $inh \times F$ . $val$ $T'$ . $syn = T'_1$ . $syn$
$T'  o \epsilon$	T'.syn = T'.inh
$F \rightarrow digit$	F.val = digit. $lexval$

## Are these SDDs S- or L-attributed?

Production	Semantic Rules
$A \rightarrow BC$	$A. a = B. b_1$ $B. b_2 = f(A. a, C. c)$

Production	Semantic Rules
$A \rightarrow BC$	$B.i = f_1(A.i)$ $C.i = f_2(B.s)$ $A.s = f_3(C.s)$

Production	Semantic Rules
$A \rightarrow BC$	$C.i = f_4(A.i)$ $B.i = f_5(C.s)$ $A.s = f_6(B.s)$

## S-Attributed and L-Attributed Definitions

Every S-attributed grammar is also a L-attributed grammar

All L-attributed grammars are not S-attributed

# Syntax-Directed Translation

## Associating Semantic Rules with Productions

- Syntax-directed definition (SDD)
  - Defines a set of attributes and translations at every node of the parse tree, output is available at the root
  - Declarative style which hides implementation details
    - Evaluation order is not specified among multiple attributes for a production
    - Only requirement is there should not be any circularity

## Associating Semantic Rules with Productions

- Syntax-directed translation (SDT)
  - Program fragments are embedded as semantic actions in production body
    - Generates code while parsing
  - Indicates order in which semantic rules are to be evaluated
  - Executable specification of an SDD, easier to implement and can be more efficient

$$rest \rightarrow +term \{ print("+") \} rest_1$$

Yacc uses translation schemes

## SDT for Infix to Postfix Translation

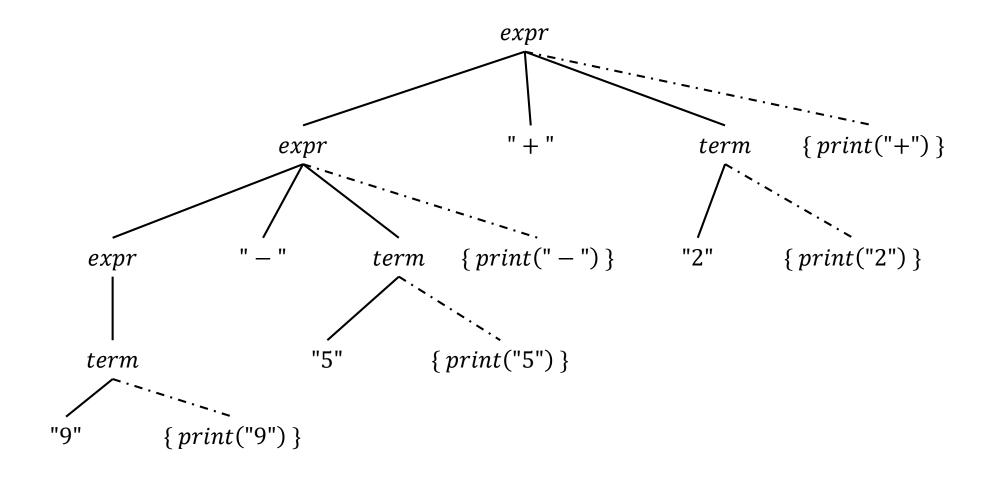
#### **SDD**

Production	Semantic Rules
$expr$ $\rightarrow expr_1 + term$	$expr.code = expr_1.code    term.code   " + "$
$expr$ $\rightarrow expr_1 - term$	$expr.code = expr_1.code    term.code   " - "$
$expr \rightarrow term$	expr.code = term.code
$term \rightarrow 0 \mid 1 \mid \mid 9$	term.code = "0" term.code = "1"  term.code = "9"

#### **SDT**

Production	Semantic Rules
$expr \rightarrow expr_1 + term$	{ print(" + ") }
$expr \rightarrow expr_1 - term$	{ print(" - ") }
$expr \rightarrow term$	
$term \rightarrow 0 \mid 1 \mid \mid 9$	{ print("0") } { print("1") } { print("9") }

## **SDT Actions**



### SDDs and SDTs

input parse dependency evaluation order for string graph semantic rules

- Evaluation of the semantic rules may
  - Generate code
  - Save information in the symbol table
  - Issue error messages
  - Perform any other activity

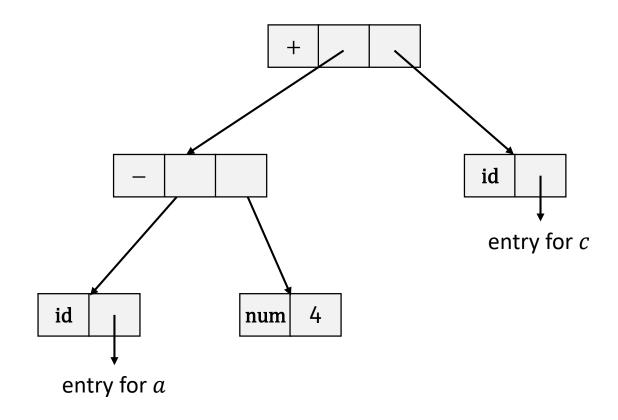
## Construction of AST for Expressions

- Idea: Construct subtrees for subexpressions by creating an operator and operand nodes
- Internal node:  $Node(op, c_1, c_2, ..., c_k)$ 
  - Create a node with label op, and k fields for k children
- Leaf node: *Leaf* (op, val)
  - Create a node with label op, and val is the lexical value

# Creating an AST

• Following sequence of function calls create an AST for a-4+c

- 1.  $p_1 = \text{new } Leaf(\text{id}, entrya)$
- 2.  $p_2 = \text{new } Leaf(\text{num}, 4)$
- 3.  $p_3 = \text{new Node}("-", p_1, p_2)$
- 4.  $p_4 = \text{new } Leaf(\text{id}, entryc)$
- 5.  $p_5 = \text{new Node}("+", p_3, p_4)$



# S-Attributed Definition for Constructing Syntax Trees

Production	Semantic Rules
$E \rightarrow E_1 + T$	???
$E \rightarrow E_1 - T$	???
$E \rightarrow T$	???
$T \to (E)$	???
T  o id	???
$T \rightarrow \mathbf{num}$	???

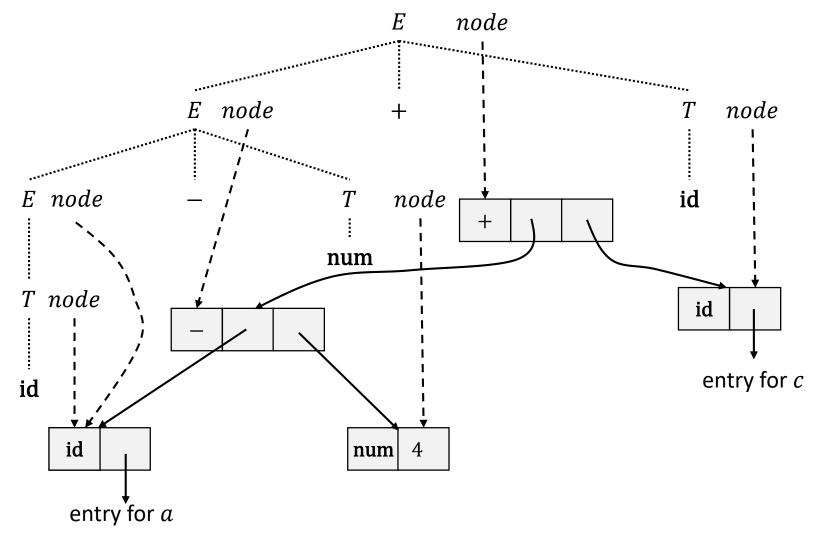
# S-Attributed Definition for Constructing Syntax Trees

Production	Semantic Rules
$E \rightarrow E_1 + T$	$E.node = \mathbf{new}  Node("+", E_1.node, T.node)$
$E \rightarrow E_1 - T$	$E.node = \mathbf{new}  Node("-", E_1.node, T.node)$
$E \rightarrow T$	E.node = T.node
$T \to (E)$	T.node = E.node
T  o id	$T.node = \mathbf{new} \ Leaf(\mathbf{id}, \mathbf{id}. \ entry)$
$T \rightarrow num$	$T.node = \mathbf{new} \ Leaf(\mathbf{num}, \mathbf{num}. \ val)$

## Construction of AST for a - 4 + c

AST edge

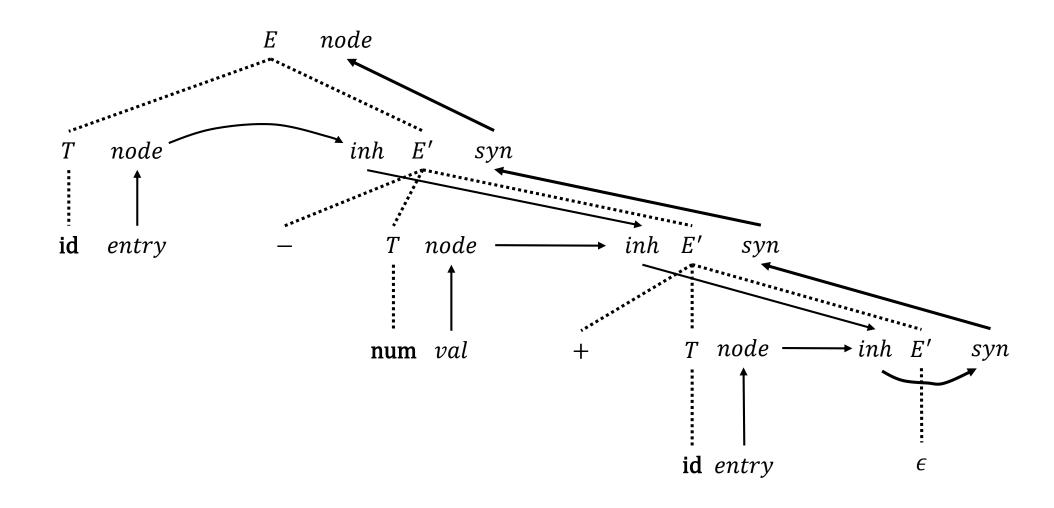
Parse Tree edge .....



# L-Attributed Definition for Constructing Syntax Trees

Production	Semantic Rules
$E \to TE'$	E.node = E'.syn E'.inh = T.node
$E' \rightarrow +TE'_1$	$E'_1.inh = new Node("+", E'.inh, T.node)$ $E'.syn = E'_1.syn$
$E' \rightarrow -TE'_1$	$E'_1.inh = new Node("-", E'.inh, T.node)$ $E'.syn = E'_1.syn$
$E' \rightarrow \epsilon$	E'.syn = E'.inh
$T \to (E)$	T.node = E.node
T  o id	$T.node = \mathbf{new}  Leaf(id, id.  entry)$
T  o num	$T.node = \mathbf{new} \ Leaf(\mathbf{num}, \mathbf{num}. \ val)$

# Dependency Graph for a - 4 + c



# Implementing SDTs

- SDTs can be implemented by
  - 1. building a parse tree
  - performing the actions in a left-to-right depth-first order, i.e., preorder traversal

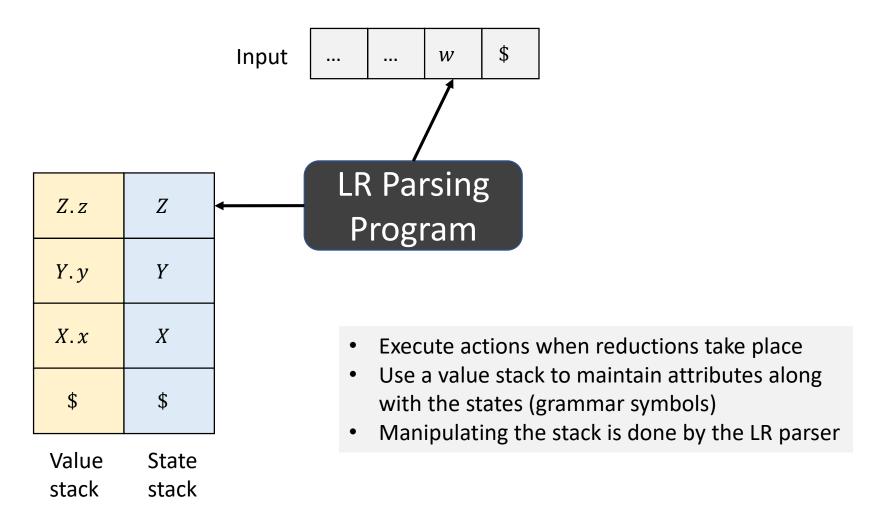
- SDTs are often implemented during parsing, but without a parse tree
  - Underlying grammar is LR, and the SDD is S-attributed
  - Underlying grammar is LL, and the SDD is L-attributed

## Postfix SDT for the Desk Calculator

- Consider S-attributed SDD for a bottom-up grammar
- We can construct an equivalent SDT with actions at the end of each production
- SDT with all actions at the rightend of a production are called postfix SDT

```
L \rightarrow E\$ { print(E.val) }
E \rightarrow E_1 + T { E.val = E_1.val + T.val }
E \rightarrow T { E.val = T.val }
T \rightarrow T_1 * F { T.val = T_1.val \times F.val }
T \rightarrow F { T.val = F.val }
F \rightarrow (E) { F.val = E.val }
F \rightarrow digit { F.val = digit.lexval }
```

# Implementing Postfix SDTs During LR Parsing



## Implementing Postfix SDTs with Bottom-up Parsing

Production	Actions
$L \to E$ \$	$\{print(stack[top-1].val); top = top-1\}$
$E \rightarrow E_1 + T$	${ stack[top-2].val = stack[top-2].val + stack[top].val; top = top-2; }$
$E \rightarrow T$	
$T \to T_1 * F$	$\{ stack[top - 2].val = stack[top - 2].val \times stack[top].val; top = top - 2; \}$
$T \to F$	
$F \to (E)$	$\{ stack[top-2].val = stack[top-1].val; top = top-2; \}$
$F \rightarrow digit$	

## SDT with Actions Inside Productions

$$B \rightarrow X \{a\} Y$$

• For bottom-up parsing, execute action  $\alpha$  as soon as X occurs on top of the stack

• For top-down parsing, execute action  $\alpha$  just before expanding nonterminal Y or checking for terminal Y in the input

# Example of an SDT Problematic for Parsing

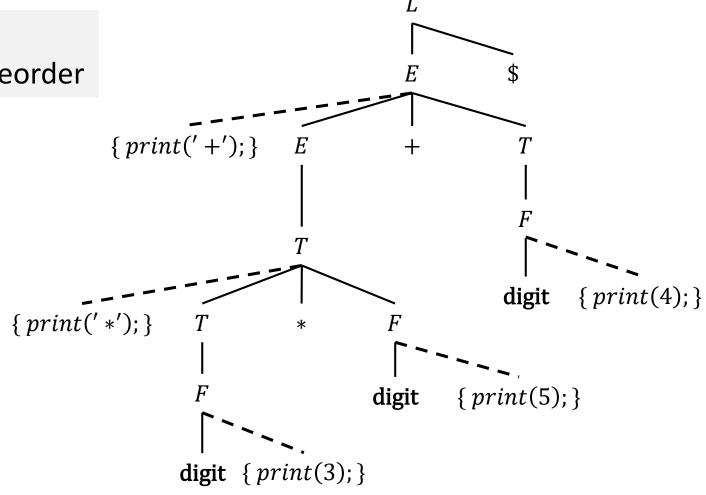
```
L \rightarrow E$
E \rightarrow \{print("+"); \} E_1 + T
E \rightarrow T
T \rightarrow \{ print("*"); \} T_1 * F
T \to F
F \rightarrow (E)
F \rightarrow digit \{ print(\mathbf{digit}, lexval); \}
```

# Implementation of Any SDT

- Parse the input and produce a parse tree
  - Ignore the actions for this step
- Examine each interior node N, say one for production  $A \to \alpha$ 
  - Add additional children to N for the actions in  $\alpha$ , in left to right order
- Perform a preorder traversal of the tree
  - Perform an action as a node labeled by an action is visited

## Parse Tree with Embedded Actions

- Parse tree for 3\*5+4
- Traverse the tree in preorder



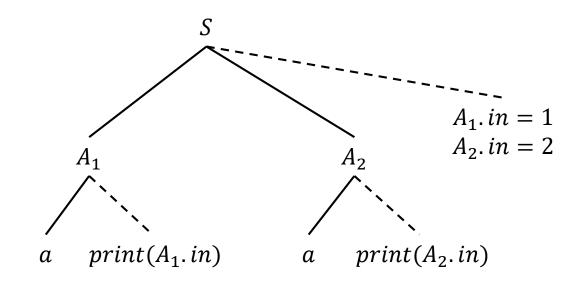
## Design of Translation Schemes

- Make all attribute values available when the semantic action is executed
- When semantic action involves only synthesized attributes, the action can be put at the end of the production

## Design of Translation Schemes

- Rules for L-attributed SDDs
  - An inherited attribute for a symbol in the body of a production must be computed in an action before the symbol
  - A synthesized attribute for the nonterminal on the LHS can only be computed when all the attributes it references have been computed
    - The action is usually put at the end of the production

$$S \to A_1 A_2 \{ A_1 . in = 1, A_2 . in = 2 \}$$
  
 $A \to a \{ print(A . in) \}$ 



What will happen on a DFS?

## References

- A. Aho et al. Compilers: Principles, Techniques, and Tools, 2<sup>nd</sup> edition, Chapter 2.3, Chapter 5.
- K. Cooper and L. Torczon. Engineering a Compiler, 2<sup>nd</sup> edition, Chapter 4.
- M. Scott. Programming Language Pragmatics, 4<sup>th</sup> edition, Chapter 4.