# CS 335: Semantic Analysis 

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## An Overview of Compilation



## Beyond Scanning and Parsing

- Example 1
std::string $x ;$
int $y$;
$y=x+3$
- Example 2
int $a, b ;$
a = b + c

```
int dot_prod(int x[], int y[]) {
    int d, i;
    d = 0;
    for (i=0; i<10; i++)
        d += x[i]*y[i];
    return d;
}
main() {
    int p, a[10], b[10];
    p = dot_prod(a,b);
}
```


## Beyond Scanning and Parsing

- A compiler must do more than just recognize whether a sentence belongs to a programming language grammar
- An input program can be grammatically correct but may contain other errors that prevent compilation
- Lexer and parser cannot catch all program errors
- Some language features cannot be modeled using context-free grammar (CFG)
- Whether a variable has been declared before use?
- Parameter types and numbers match in the declaration and use of a function
- Types match on both sides of an assignment


## Limitations with CFGs

$$
\text { ProcedureBody } \rightarrow \text { Declarations Executables }
$$

- CFGs deal with syntactic categories rather than specific words
- Grammar can specify the positions in an expression where a variable name may occur
- Enforcing the "declare before use" rule requires knowledge that cannot be encoded in a CFG
- CFG cannot match one instance of a variable name with another


## Questions That Compiler Needs to Answer

Questions $\left\{\begin{array}{l}\text { - Has a variable been declared? } \\ \text { - What is the type and size of a variable? } \\ \text { - Is the variable scalar or an array? } \\ \text { - Is an array access } A[i][j][\mathrm{k}] \text { consistent with the declaration? } \\ \text { - Does the name " } x \text { " correspond to a variable or a function? } \\ \text { - If } x \text { is a function, how many arguments does it take? } \\ \text { - What kind of value, if any, does a function } x \text { return? } \\ \text { - Are all invocations of a function consistent with the } \\ \text { declaration? } \\ \text { - Track inheritance relationship } \\ \text { - Ensure that classes and its methods are not multiply defined }\end{array}\right.$

## Questions That Compiler Needs to Answer

```
x}\leftarrowy+
```

$$
x \leftarrow a+b
$$

Compilers need to understand the structure of the computation to translate the input program

## Semantic Analysis

- Finding answers to these questions is part of the semantic analysis phase
- For example, ensure variable are declared before their uses and check that each expression has a correct type
- These are static semantics of languages


## Checking Dynamic Semantics

- Dynamic semantics of languages need to be checked at run time
- Whether an overflow will occur during an arithmetic operation?
- Whether array bounds will be exceeded during execution?
- Whether recursion will exceed stack limits?
- Compilers can generate code to check dynamic semantics

```
int dot_prod(int x[], int y[]) {
    int d, i;
    d = 0;
    for (i=0; i<10; i++)
        d += x[i]*y[i];
    return d;
}
```

```
main() {
```

main() {
int p; int a[10], b[10];
int p; int a[10], b[10];
p = dot_prod(a,b);
p = dot_prod(a,b);
}

```
}
```


## How does a compiler answer these questions?

- Compilers track additional information for semantic analysis
- For example, types of variables, function parameters, and array dimensions
- Type information is stored in the symbol table or the syntax tree
- Used not only for semantic validation but also for subsequent phases of compilation
- The information required may be non-local in some cases
- Semantic analysis can be performed during parsing or in another pass that traverses the IR produced by the parser


## How does a compiler answer these questions?

- Use formal methods like context-sensitive grammars
- Use ad-hoc techniques using symbol table
- Static semantics of PL can be specified using attribute grammars
- Attribute grammars are extensions of context-free grammars

Attribute Grammar Framework

## Syntax-Directed Definition

- A syntax-directed definition (SDD) is a context-free grammar with rules and attributes
- A SDD specifies the values of attributes by associating semantic rules with the grammar productions

| Production | Semantic Rule |
| :---: | :---: |
| $E \rightarrow E_{1}+T$ | $E . \operatorname{code}=E_{1} \cdot \operatorname{code}\\|T \cdot \operatorname{code}\\| "+"$ |

- Attribute grammars are SDDs with no side effects


## Syntax-Directed Definition

- Generalization of CFG where each grammar symbol has an associated set of attributes
- Let $G=(T, N T, S, P)$ be a CFG and let $V=T \cup N T$
- Every symbol $X \in V$ is associated with a set of attributes (for e.g., denoted by $X . a$ and $X . b)$
- Each attribute takes values from a specified domain (finite or infinite), which is its type
- Typical domains of attributes are, integers, reals, characters, strings, booleans, and structures
- New domains can be constructed from given domains by mathematical operations such as cross product and map
- Values of attributes are computed by semantic rules


## Example

- Consider a grammar for signed binary numbers

```
number }->\mathrm{ sign list
sign }->+|
list }->\mathrm{ list bit | bit
bit }->0|
```

- Build attribute grammar that annotates Number with the value it represents


## Example

- Consider a grammar for signed binary numbers

```
number }->\mathrm{ sign list
sign }->+|
list }->\mathrm{ list bit | bit
bit }->0|
```

- Build attribute grammar that annotates number with the value it represents
- Associate attributes with grammar symbols


## Example Attribute Grammar

| Production | Attribute Rule |
| :---: | :---: |
| number $\rightarrow$ sign list | ```list.pos \(=0\) if sign.neg: number.val \(=-l i s t . v a l\) else: number.val \(=-l i s t . v a l\)``` |
| $\operatorname{sign} \rightarrow+$ | sign. $n$ eg $=$ false |
| sign $\rightarrow$ - | sign.neg = true |
| list $\rightarrow$ bit | $\begin{aligned} & \text { bit. } . \text { os }=\text { list. } \mathrm{pos} \\ & \text { list.val }=\text { bit.val } \end{aligned}$ |
| list $_{0} \rightarrow$ list $_{1}$ bit | $\begin{aligned} & \text { list }_{1} \cdot \text { pos }=\text { list }_{0} \cdot \text { pos }+1 \\ & \text { bit.pos }=\text { list }_{0} \cdot \text { pos } \\ & \text { list }_{0} \cdot v a l=\text { list }_{1} \cdot v a l+\text { bit.val } \end{aligned}$ |
| bit $\rightarrow 0$ | bit.val $=0$ |
| bit $\rightarrow 1$ | bit.val $=2^{\text {bit.pos }}$ |

## Parse Tree



## Annotated Parse Tree

- A parse tree showing the value(s) of its attribute(s) is called an annotated parse tree



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## Dependency Graph

- If an attribute $b$ depends on an attribute $c$ then the semantic rule for $b$ must be evaluated after the semantic rule for $c$
- The dependencies among the nodes are depicted by a directed graph called dependency graph


## Dependency Graph

- Suppose A. $a=f(X . x, Y . y)$ is a semantic rule for $A \rightarrow X Y$

- Suppose $X . x=f(A . a, Y . y)$ is a semantic rule for $A \rightarrow X Y$



## Construct Dependency Graph

for each node $n$ in the parse tree do
for each attribute $a$ of the grammar symbol do construct a node in the dependency graph for $a$
for each node $n$ in the parse tree do
for each semantic rule $b=f\left(c_{1}, c_{2}, \ldots, c_{k}\right)$ do for $i=1$ to $k$ do
construct an edge from $c_{i}$ to $b$
// Associated with production at node $n$

## Evaluating an SDD

- In what order do we evaluate attributes?
- SDDs do not specify any order of evaluation
- We must evaluate all the attributes upon which the attribute of a node depends
- Any topological sort of dependency graph gives a valid order in which semantic rules must be evaluated
- For SDD's with both synthesized and inherited attributes, there is no guarantee of an order of evaluation existing


## Evaluating an SDD

- Parse tree method
- Use topological sort of the dependency graph to find the evaluation order
- Rule-based method
- Semantic rules are analyzed and order of evaluation is predetermined
- Oblivious method
- Evaluation order ignores the semantic rules


## Circular Dependency of Attributes

Production
Semantic Rules
$A \rightarrow B$ A. $s=B . i$
B. $i=A . s+1$


## Types of Nonterminal Attributes

## Synthesized

- Value of a synthesized attribute for a nonterminal $A$ at a node $N$ is computed from the values of children nodes and $N$ itself
- Defined by a semantic rule associated with a production at $N$ such that the production has $A$ as its head


## Inherited

- Value of an inherited attribute for a nonterminal $B$ at a node $N$ is computed from the values at $N$ 's parent, $N$ itself, and $N$ 's siblings
- Defined by a semantic rule associated with the production at the parent of $N$ such that the production has $B$ in its body


## Syntax-Directed Definition

- A grammar production $A \rightarrow \alpha$ has an associated semantic rule $b=$ $f\left(c_{1}, c_{2}, \ldots, c_{k}\right)$
- $b$ is a synthesized attribute of $A$ and $c_{1}, c_{2}, \ldots, c_{k}$ are attributes of symbols in the production
- $b$ is an inherited attribute of a symbol in the body, and $c_{1}, c_{2}, \ldots, c_{k}$ are attributes of symbols in the production
- Start symbol does not have inherited attributes


## Terminal Attributes

- Terminals can have synthesized attributes, but not inherited attributes
- Attributes for terminals have lexical values that are supplied by the lexical analyzer


## Postfix Notation

- Postfix notation for an expression $E$ is defined inductively
- If $E$ is a variable or constant, then postfix notation is $E$
- If $E=E_{1} \mathrm{op} E_{2}$ where op is any binary operator, then the postfix notation is $E_{1}^{\prime} E_{2}^{\prime} \mathrm{op}$, where $E_{1}^{\prime}$ and $E_{2}^{\prime}$ are postfix notations for $E_{1}$ and $E_{2}$ respectively
- If $E=\left(E_{1}\right)$, then postfix notation for $E_{1}$ is the notation for $E$


## SDD for Infix to Postfix Translation

| Production | Semantic Rules |
| :---: | :---: |
| expr $\rightarrow$ expr ${ }_{1}+$ term | expr.code $=$ expr $_{1} \cdot$ code $\\|$ term. code\\| $\mid$ "+" |
| expr $\rightarrow$ expr ${ }_{1}$ - term | expr.code $=$ expr $_{1} . \operatorname{code\\| } \\|$ term.code\\||" ${ }^{\text {- }}$ |
| expr $\rightarrow$ term | expr.code $=$ term. code |
| term $\rightarrow 0\|1\| \ldots \mid 9$ | $\begin{aligned} & \text { term. } \operatorname{code}=" 0 " \\ & \text { term. code }=" 1 " \\ & \ldots \\ & \text { term. } \operatorname{code}=" 9 " \end{aligned}$ |

## Annotated Parse Tree



## Types of SDDs

- Arbitrary SDDs can have cycles
- Cycles need to be avoided
- Can no longer meaningfully proceed with evaluation
- Expensive to detect
- Two types of SDDs guarantee no cycles
- S-attributed and L-attributed


## S-Attributed Definition

- An SDD that involves only synthesized attributes is called S-attributed definition
- Each rule computes an attribute for the head nonterminal from attributes taken from the body of the production
- Semantic rules in a S-attributed definition can be evaluated by a bottom-up or postorder traversal of the parse tree
- An S-attributed SDD can be implemented naturally in conjunction with an LR parser


## Example SDD

| Production | Semantic Rules |
| :---: | :--- |
| $L \rightarrow E \$$ | L.val $=E . v a l$ |
| $E \rightarrow E_{1}+T$ | $E . v a l=E_{1} . v a l+T . v a l$ |
| $E \rightarrow T$ | $E . v a l=T . v a l$ |
| $T \rightarrow T_{1} * F$ | $T . v a l=T_{1} . v a l \times F . v a l$ |
| $T \rightarrow F$ | $T . v a l=F . v a l$ |
| $F \rightarrow(E)$ | F.val $=E . v a l$ |
| $F \rightarrow$ digit | F.val $=$ digit. lexval |

## Annotated Parse Tree for $3 * 5+4 \$$



## Abstract Syntax Tree (AST)

- Condensed form of a parse tree used for representing language constructs
- ASTs do not check for string membership in the language for a grammar
- ASTs represent relationships between language constructs, do not bother with derivations

$$
S \rightarrow \text { if } P \text { then } S_{1} \text { else } S_{2}
$$



- Parse trees are also called concrete syntax trees


## Parse Tree and Abstract Syntax Tree

Parse Tree



Abstract Syntax Tree


## Inherited Attributes

- Useful when the structure of the parse tree does not match the abstract syntax of the source code

| Production | Semantic Rules |
| :---: | :---: |
| $T \rightarrow F T^{\prime}$ | $\begin{aligned} & T^{\prime} . i n h=F . \text { val } \\ & T . v a l=T^{\prime} . \text { syn } \end{aligned}$ |
| $T^{\prime} \rightarrow * F T_{1}^{\prime}$ | $\begin{aligned} & T_{1}^{\prime} \cdot i n h=T^{\prime} \cdot i n h \times F \cdot v a l \\ & T^{\prime} \cdot \operatorname{syn}=T_{1}^{\prime} \cdot \text { syn } \end{aligned}$ |
| $T^{\prime} \rightarrow \epsilon$ | $T^{\prime}$. syn $=T^{\prime} . \mathrm{inh}$ |
| $F \rightarrow$ digit | F.val $=$ digit. lexval |

## Parse Tree and Annotated Parse Tree for $3 * 5$



## Parse Tree and Annotated Parse Tree for $3 * 5$



## Another Example

## Parse Tree for "float $x, y, z$ "

| Production | Semantic Rules |
| :---: | :--- |
| $D \rightarrow T L$ | L.in $=$ T.type |
| $T \rightarrow$ float | T.type $=$ float |
| $T \rightarrow$ int | T.type $=$ int |
| $L \rightarrow L_{1}$, id | $L_{1}$. in $=$ L.in; addtype(id. entry,L.in $)$ |
| $L \rightarrow$ id | addtype(id.entry,L.in $)$ |

addtype () installs $L$. in as the type of the symbol table object pointed to by id. entry


## Dependency Graph for float $x, y, z$



## Evaluating S-Attributed Definitions

- Attributes can be evaluated with a postorder traversal of the parse tree

```
postorder(N) {
    for (each child C of N, from left to right)
        postorder(C)
    evaluate the attributes associated with node N
}
```


## Notes about Inherited Attributes

- Always possible to rewrite a SDD to use only synthesized attributes
- Inherited attributes can be simulated with synthesized attributes
- May be more logical to use both synthesized and inherited attributes
- Inherited attributes usually cannot be evaluated by a simple preorder traversal of the parse tree
- Attributes may depend on both left and right siblings!
- Attributes that do not depend from right children can be evaluated by a preorder traversal


## Bottom-up Evaluation of S-Attributed Definitions

- Suppose $A \rightarrow X Y Z$, and semantic rule is $A . a=$ $f(X . x, Y . y, Z . z)$
- Can be computed during bottom-up parsing
- On reduction, value of new synthesized attribute $A$. $a$ is computed from the attributes on the stack
- Extend stack to hold values



## Example S-Attributed Definition

| Production | Semantic Rules |
| :---: | :--- |
| $L \rightarrow E \$$ | L.val $=E . v a l$ |
| $E \rightarrow E_{1}+T$ | $E . v a l=E_{1} . v a l+T . v a l$ |
| $E \rightarrow T$ | $E . v a l=T . v a l$ |
| $T \rightarrow T_{1} * F$ | $T . v a l=T_{1} . v a l \times F . v a l$ |
| $T \rightarrow F$ | $T . v a l=F . v a l$ |
| $F \rightarrow(E)$ | F.val $=E . v a l$ |
| $F \rightarrow$ digit | F.val $=$ digit. lexval |

## Bottom-up Evaluation of S-Attributed Definitions

| Value | State | Action |  |
| :--- | :--- | ---: | :--- |
| $\$$ | $\$$ | $3 * 5+4 \$$ | Shift |
| $\$ 3$ | $\$$ digit | $* 5+4 \$$ | Reduce by $F \rightarrow$ digit |
| $\$ 3$ | $\$ F$ | $* 5+4 \$$ | Reduce by $T \rightarrow F$ |
| $\$ 3$ | $\$ T$ | $* 5+4 \$$ | Shift |
| $\$ 3$ | $\$ T *$ | $5+4 \$$ | Shift |
| $\$ 35$ | $\$ T *$ digit | $+4 \$$ | Reduce by $F \rightarrow$ digit |
| $\$ 35$ | $\$ T * F$ | $+4 \$$ | Reduce by $T \rightarrow T * F$ |
| $\$ 15$ | $\$ T$ | $+4 \$$ | Reduce by $E \rightarrow T$ |
| $\$ 15$ | $\$ E$ | $+4 \$$ | Shift |
| $\$ 15$ | $\$ E+$ | $4 \$$ | Shift |
| $\$ 154$ | $\$ E+$ digit | $\$$ | Reduce by $F \rightarrow$ digit |
| $\$ 154$ | $\$ E+F$ | $\$$ | Reduce by $T \rightarrow F$ |
| $\$ 154$ | $\$ E+T$ | $\$$ | Reduce by $E \rightarrow E+T$ |
| $\$ 19$ | $\$ E$ | $\$$ | $\ldots$ |
| CS 335 |  |  |  |

## L-Attributed Definitions

- Each attribute must be either
I. Synthesized
II. Suppose $A \rightarrow X_{1} X_{2} \ldots X_{n}$ and $X_{i} . a$ is an inherited attribute. $X_{i}$. a can be computed using
a) Only inherited attributes from $A$, or
b) Either inherited or synthesized attributes associated with $X_{1}, \ldots, X_{i-1}$, or
c) Inherited or synthesized attributes
associated with $X_{i}$.

| Production | Semantic Rules |
| :---: | :---: |
| $T \rightarrow F T^{\prime}$ | $\begin{aligned} & T^{\prime} \cdot \mathrm{inh}=F \cdot \mathrm{val} \\ & T . v a l=T^{\prime} . s y n \end{aligned}$ |
| $T^{\prime} \rightarrow * F T_{1}^{\prime}$ | $\begin{aligned} & T_{1}^{\prime} \cdot i n h=T^{\prime} \cdot \operatorname{inh} \times F \cdot v a l \\ & T^{\prime} \cdot \operatorname{syn}=T_{1}^{\prime} \cdot s y n \end{aligned}$ |
| $T^{\prime} \rightarrow \epsilon$ | $T^{\prime} . \operatorname{syn}=T^{\prime}$. inh |
| $F \rightarrow$ digit | F.val = digit. lexval |

## Are these SDDs S- or L-attributed?

| Production | Semantic Rules |
| :---: | :--- |
| $A \rightarrow B C$ | A. $a=B \cdot b_{1}$ <br> $B \cdot b_{2}=f(A \cdot a, C . c)$ |


| Production | Semantic Rules |
| :---: | :---: |
| $A \rightarrow B C$ | $\begin{aligned} & B . i=f_{1}(A . i) \\ & C . i=f_{2}(B . s) \\ & A . s=f_{3}(C . s) \end{aligned}$ |
| Production | Semantic Rules |
| $A \rightarrow B C$ | $\begin{aligned} & C . i=f_{4}(A . i) \\ & B . i=f_{5}(C . s) \\ & A . s=f_{6}(B . s) \end{aligned}$ |

## S-Attributed and L-Attributed Definitions

Every S-attributed grammar is also a L-attributed grammar

All L-attributed grammars are not S-attributed

## Syntax-Directed Translation

## Associating Semantic Rules with Productions

- Syntax-directed definition (SDD)
- Defines a set of attributes and translations at every node of the parse tree, output is available at the root
- Declarative style which hides implementation details
- Evaluation order is not specified among multiple attributes for a production
- Only requirement is there should not be any circularity


## Associating Semantic Rules with Productions

- Syntax-directed translation (SDT)
- Program fragments are embedded as semantic actions in production body
- Generates code while parsing
- Indicates order in which semantic rules are to be evaluated
- Executable specification of an SDD, easier to implement and can be more efficient

$$
\text { rest } \rightarrow+\text { term }\{\operatorname{print}("+")\} \text { rest }_{1}
$$

- Yacc uses translation schemes


## SDT for Infix to Postfix Translation

|  | SDD | SDT |  |
| :---: | :---: | :---: | :---: |
| Production | Semantic Rules | Production | Semantic Rules |
| $\underset{\rightarrow \text { expr }}{1}+\text { term }$ | ```expr.code = expr..code\|term.code||"+"``` | expr $\rightarrow$ expr ${ }_{1}+$ term | $\{\operatorname{print}($ " + ") $\}$ |
| $\underset{\rightarrow \text { expr }}{1}-\operatorname{term}$ | $\begin{aligned} & \text { expr.code }= \\ & \text { expr }_{1} \cdot \operatorname{code} \\| \text { term.code } \\| "-" \end{aligned}$ | expr $\rightarrow$ expr $r_{1}-$ term expr $\rightarrow$ term | $\left\{\operatorname{print}\left({ }^{\prime}-{ }^{\prime \prime}\right)\right.$ \} |
| expr $\rightarrow$ term | expr.code $=$ term. code |  | \{print("0") \} |
| term $\rightarrow 0\|1\| \ldots \mid 9$ | $\begin{aligned} & \text { term. code }=" 0 " \\ & \text { term. code }=" 1 " \\ & \ldots \\ & \text { term. } \operatorname{code}=" 9 " \end{aligned}$ | term $\rightarrow 0\|1\| \ldots \mid 9$ | $\begin{aligned} & \{\operatorname{print}(" 1 ")\} \\ & \{ \\ & \{\operatorname{print}(" 9 ")\} \end{aligned}$ |

## SDT Actions



## SDDs and SDTs



- Evaluation of the semantic rules may
- Generate code
- Save information in the symbol table
- Issue error messages
- Perform any other activity


## Construction of AST for Expressions

- Idea: Construct subtrees for subexpressions by creating an operator and operand nodes
- Internal node: Node (op, $\left.c_{1}, c_{2}, \ldots, c_{k}\right)$
- Create a node with label $o p$, and $k$ fields for $k$ children
- Leaf node: Leaf(op, val)
- Create a node with label $o p$, and $v a l$ is the lexical value


## Creating an AST

- Following sequence of function calls create an AST for $a-4+c$

1. $\quad p_{1}=$ new $\operatorname{Leaf}(\mathrm{id}$, entrya)
2. $p_{2}=$ new $\operatorname{Leaf}$ (num, 4)
3. $p_{3}=$ new $\operatorname{Node}\left("-{ }^{\prime \prime}, p_{1}, p_{2}\right)$
4. $\quad p_{4}=$ new $\operatorname{Leaf}(\mathrm{id}$, entryc)
5. $p_{5}=$ new $\operatorname{Node}\left("+{ }^{\prime \prime}, p_{3}, p_{4}\right)$


## S-Attributed Definition for Constructing Syntax Trees

| Production |  |
| :---: | :--- |
| $E \rightarrow E_{1}+T$ | $? ? ?$ |
| $E \rightarrow E_{1}-T$ | $? ? ?$ |
| $E \rightarrow T$ | $? ? ?$ |
| $T \rightarrow(E)$ | $? ? ?$ |
| $T \rightarrow$ id | $? ? ?$ |
| $T \rightarrow$ num | $? ? ?$ |

## S-Attributed Definition for Constructing Syntax Trees

| Production | Semantic Rules |
| :---: | :---: |
| $E \rightarrow E_{1}+T$ |  |
| $E \rightarrow E_{1}-T$ |  |
| $E \rightarrow T$ | E. $\mathrm{node}=$ T. node |
| $T \rightarrow(E)$ | T. node = E.node |
| $T \rightarrow$ id | T. node $=$ new Leaf (id, id. entry) |
| $T \rightarrow$ num | T. node $=$ new Leaf(num, num. val) |

## Construction of AST for $a-4+c$

$\qquad$


## L-Attributed Definition for Constructing Syntax Trees

| Production | Semantic Rules |
| :---: | :---: |
| $E \rightarrow T E^{\prime}$ | $\begin{aligned} & E . \text { node }=E^{\prime} . \text { syn } \\ & E^{\prime} . \operatorname{inh}=T . \text { node } \end{aligned}$ |
| $E^{\prime} \rightarrow+T E_{1}^{\prime}$ | $\begin{aligned} & E_{1}^{\prime} \cdot \operatorname{inh}=\text { new } N o d e\left("+", E^{\prime} \cdot i n h, T \cdot n o d e\right) \\ & E^{\prime} \cdot \operatorname{syn}=E_{1}^{\prime} \cdot \text { syn } \end{aligned}$ |
| $E^{\prime} \rightarrow-T E_{1}^{\prime}$ | $\begin{aligned} & E_{1}^{\prime} \cdot \text { inh }=\text { new } \operatorname{Node}\left("-", E^{\prime} \cdot \text { inh }, T \cdot n o d e\right) \\ & E^{\prime} \cdot \text { syn }=E_{1}^{\prime} \cdot \text { syn } \end{aligned}$ |
| $E^{\prime} \rightarrow \epsilon$ | $E^{\prime}$. syn $=E^{\prime} . \mathrm{inh}$ |
| $T \rightarrow(E)$ | T. node $=$ E.node |
| $T \rightarrow$ id | T. node $=$ new Leaf(id, id. entry) |
| $T \rightarrow$ num | T. node $=$ new Leaf(num, num. val) |

## Dependency Graph for $a-4+c$



## Implementing SDTs

- SDTs can be implemented by

1. building a parse tree
2. performing the actions in a left-to-right depth-first order, i.e., preorder traversal

- SDTs are often implemented during parsing, but without a parse tree
- Underlying grammar is LR, and the SDD is S-attributed
- Underlying grammar is LL, and the SDD is L-attributed


## Postfix SDT for the Desk Calculator

- Consider S-attributed SDD for a bottom-up grammar
- We can construct an equivalent SDT with actions at the end of each production
- SDT with all actions at the rightend of a production are called postfix SDT

$$
\begin{array}{ll}
L \rightarrow E \$ & \{\text { print }(E . v a l)\} \\
E \rightarrow E_{1}+T & \left\{E . v a l=E_{1} \cdot v a l+T . v a l\right\} \\
E \rightarrow T & \{E . v a l=T . v a l\} \\
T \rightarrow T_{1} * F & \left\{T . v a l=T_{1} \cdot v a l \times F . v a l\right\} \\
T \rightarrow F & \{\text { T.val }=\text { F.val }\} \\
F \rightarrow(E) & \{F . v a l=E \cdot v a l\} \\
F \rightarrow \text { digit } & \{F . v a l=\text { digit. } \text { lexval }\}
\end{array}
$$

## Implementing Postfix SDTs During LR Parsing



## Implementing Postfix SDTs with Bottom-up Parsing

| Production | Actions |
| :---: | :---: |
| $L \rightarrow E \$$ | \{print(stack[top - 1].val); top = top -1$\}$ |
| $E \rightarrow E_{1}+T$ | $\begin{aligned} & \{\text { stack }[\text { top }-2] \cdot v a l=\text { stack }[\text { top }-2] \cdot v a l+ \\ & \text { stack }[\text { top }] \cdot v a l ; \text { top }=\text { top }-2 ;\} \end{aligned}$ |
| $E \rightarrow T$ |  |
| $T \rightarrow T_{1} * F$ | $\begin{aligned} & \text { \{stack }[\text { top }-2] . \text { val }=\operatorname{stack}[\text { top }-2] . v a l \times \\ & \text { stack }[\text { top }] . v a l ; \text { top }=\text { top }-2 ;\} \end{aligned}$ |
| $T \rightarrow F$ |  |
| $F \rightarrow(E)$ | $\begin{aligned} & \{\text { stack }[\text { top }-2] . v a l=\operatorname{stack}[t o p-1] . v a l ; \text { top }= \\ & \text { top }-2 ;\} \end{aligned}$ |
| $F \rightarrow$ digit |  |

## SDT with Actions Inside Productions

$$
B \rightarrow X\{a\} Y
$$

- For bottom-up parsing, execute action $a$ as soon as $X$ occurs on top of the stack
- For top-down parsing, execute action $a$ just before expanding nonterminal $Y$ or checking for terminal $Y$ in the input


## Example of an SDT Problematic for Parsing

$$
\begin{aligned}
& L \rightarrow E \$ \\
& E \rightarrow\{\operatorname{print}("+") ;\} \quad E_{1}+T \\
& E \rightarrow T \\
& T \rightarrow\{\operatorname{print}(" * ") ;\} \quad T_{1} * F \\
& T \rightarrow F \\
& F \rightarrow(E) \\
& F \rightarrow \text { digit }\{\operatorname{print}(\text { digit. lexval); }\}
\end{aligned}
$$

## Implementation of Any SDT

- Parse the input and produce a parse tree
- Ignore the actions for this step
- Examine each interior node $N$, say one for production $A \rightarrow \alpha$
- Add additional children to $N$ for the actions in $\alpha$, in left to right order
- Perform a preorder traversal of the tree
- Perform an action as a node labeled by an action is visited


## Parse Tree with Embedded Actions

- Parse tree for $3 * 5+4$
- Traverse the tree in preorder



## Design of Translation Schemes

- Make all attribute values available when the semantic action is executed
- When semantic action involves only synthesized attributes, the action can be put at the end of the production


## Design of Translation Schemes

- Rules for L-attributed SDDs
- An inherited attribute for a symbol in the body of a production must be computed in an action before the symbol
- A synthesized attribute for the nonterminal on the LHS can only be computed when all the attributes it references have been computed
- The action is usually put at the end of the production



## References

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